

BHAKTA KAVI NARSINH MEHTA UNIVERSITY JUNAGADH 362263

SYLLABUS



**Faculty of Science
M.Sc. - Mathematics
Semester – II
Under Choice Based Credit System (CBCS)
Effective From June – 2019**

Department of Mathematic

Bhakta Kavi Narsinh Mehta University Junagadh

SYLLABUS

M. Sc. (Mathematics)

(CBCS)
With effect from June-2019



DEPARTMENT OF MATHEMATICS

Course Structure and Scheme of Examination For Choice based Credit System (CBCS)

(With effect from June-2019)

- **Course :** M.Sc. (Mathematics)
- **Eligibility of the admission :** - B.Sc. (Mathematics)
- **Duration :** - Two Years

Semester 1

Subject Code	Title of the Course	Course Credits	No. of Hrs. Per Week	Weightage For Internal Examination	Weightage For Semester End Examination	Total Marks	Duration Of Semester end Exam in hrs.
CMT – 1001	Algebra 1	4	4	30	70	100	2.5hrs
CMT – 1002	Real Analysis	4	4	30	70	100	2.5hrs
CMT – 1003	Topology 1	4	4	30	70	100	2.5hrs
CMT – 1004	Theory of Ordinary Differential Equations	4	4	30	70	100	2.5hrs
CMT – 1005	Seminar and Problem Session	4	4	-	100	100	-
EMT – 1001	Classical Mechanics 1	4	4	30	70	100	2.5hrs
Total		24				600	

Semester 2

Subject Code	Title of the Course	Course Credits	No. of Hrs. Per Week	Weightage For Internal Examination	Weightage For Semester End Examination	Total Marks	Duration Of Semester end Exam in hrs.
CMT – 2001	Algebra 2	4	4	30	70	100	2.5hrs
CMT – 2002	Complex Analysis	4	4	30	70	100	2.5hrs
CMT – 2003	Topology 2	4	4	30	70	100	2.5hrs
CMT – 2004	Methods in Partial Differential Equations	4	4	30	70	100	2.5hrs
CMT – 2005	Seminar and Problem Session	4	4	-	100	100	-
EMT – 2001	Classical Mechanics 2	4	4	30	70	100	2.5hrs
Total		24				600	

M.Sc.(Mathematics) - SEMESTER 1

CMT - 1001 Algebra- I

CMT - 1002 Real Analysis

CMT - 1003 Topology- I

CMT - 1004 Theory of Ordinary Differential Equations

CMT - 1005 Seminar and Problem Session

EMT - 1001 Classical Mechanics- I

M.Sc.(Mathematics) - SEMESTER 2

CMT - 2001 Algebra- II

CMT - 2002 Complex Analysis

CMT - 2003 Topology- II

CMT - 2004 Methods in Partial Differential Equations

CMT - 2005 Seminar and Problem Session

EMT - 2001 Classical Mechanics- II

* CMT – Core Subject, EMT –Elective Subject, PMT - Practical

- Passing Standard is 40% in Internal as well as in external examinations for all the courses.
- Student will have to clear internal as well as external examinations. (i.e. internal examination with minimum 40% and external examination with minimum 40% is compulsory) and student can earn credits mentioned against each course.
- There will be two internal examinations in each course and average of both the examinations will be considered.

M.Sc. SEMESTER 2

Sub. Code: **CMT-2001**

Core Sub. 1: **Algebra- 2**

Unit 1

Division ring and Field, Extension fields, algebraic and transcendental extensions, Splitting fields, Normal extensions, Multiple roots, Finite fields, Separable extensions.

Unit 2

Automorphism fixed fields, Galois extension, Fundamental theorem of Galois Theory, Fundamental theorem of Algebra.

Unit 3

Modules (Definitions and examples), Submodules and Operation on modules

Unit 4

Homomorphisms of modules and quotient modules, completely reducible modules, finitely generated modules.

Reference Books:

- 1) P. B. Bhattacharya, S. K. Jain and S. R. Nagpaul, Basic Abstract Algebra, Second Edition, Cambridge University Press, 1995.
- 2) M. Artin, Algebra, Prentice-Hall of India Private Ltd., New Delhi, 1994.
- 3) J. A. Gallian, Contemporary Abstract Algebra, Fourth Edition, Narosa Publishing House, New Delhi, 1999.
- 4) N. S. Gopalakrishnan, University Algebra, New Age International Private Ltd. Publishers, New Delhi, Sixth Reprint, 1998.
- 5) I. N. Herstein, Topics in Algebra, Second Edition, Wiley Pub. , New York, 1975.

M.Sc. SEMESTER 2

Sub. Code: **CMT-2002**

Core Sub. 2: **Complex Analysis**

Unit 1

The extended complex plane and its spherical representation, analytic functions, bilinear transformations, their properties and classifications, Branches of many valued functions with special reference to $\arg z$, $\log z$ and z^a , elementary Riemann surfaces, definition and properties of conformal mapping.

Unit 2

Riemann – Steiltjes integral and its properties, line integral and its properties, fundamental theorem of calculus for line integral, Leibnitz rule, Taylor's theorem, Cauchy's integral formula and Cauchy's theorem for analytic functions on an open disc, winding number of a closed rectifiable curve with respect to a point outside the curve and its properties, Cauchy's integral formula first version and second version, Cauchy's theorem first version, second version, third version and fourth version.

Unit 3

Cauchy – Goursat theorem, Morera's theorem, Cauchy's inequality, entire functions, Liouville's theorem, identity theorem, fundamental theorem of algebra, maximum modulus theorem and minimum modulus theorem.

Unit 4

Schwarz lemma, meromorphic functions, argument principle, Rouché's theorem, Open Mapping Theorem, Inverse function theorem.

Unit 5

Isolated singularities, classifications of singularities, Laurent's series, residue theorem, evaluation of integrals.

This course is covered by relevant portions from the text **“Functions of One Complex Variable”** by John B. Conway, Third Edition, Springer International Student Edition, Narosa Publishing House.

Reference Books:-

- 1) Complex Analysis by L. V. Ahlfors, International Student Edition, Mc Graw – Hill Book Company, 1979.
- 2) Complex Analysis by Karunakaran, Second Edition, Narosa Publishing House, 2006.
- 3) A First Course in Complex Analysis with Applications by Dennis G. Zill and Patrik D. Shanahan, Second Edition, Jones & Bartlett Student Edition, 2010.
- 4) Complex Analysis by S. Lang, Addison-Wesley, 1977.
- 5) Foundations of Complex Analysis by S. Ponnusamy, Narosa Publishing House, 1977.
- 6) Fundamentals of Complex Analysis with Applications to Engineering and Science by E. B. Saff and A. D. Snider, Third Edition, Pearson Education.
- 7) Notes on Complex Function Theory by D. Sarasan, Hindustan Book Agency, 1994.

M.Sc. SEMESTER 2

Sub. Code: **CMT-2003**

Core Sub. 3: **Topology- 2**

Unit – 1:

Separation Axioms: T_1 – Spaces, T_2 – Spaces (Hausdorff Spaces).

Unit – 2:

Separation Axioms: Regular Spaces, Completely Regular Spaces, Normal Spaces.

Unit – 3:

Compact Spaces, Locally Compact Spaces, Limit Point Compact Spaces.

Unit – 4:

Sequentially Compact Spaces, Compact Metric Spaces.

Unit – 5:

Complete Metric Spaces.

Reference Books:-

- 1) Topology – A First Course, J.R.Munkres, Prentice Hall of India (2000). Chapter 3 (Article no. 26 to 29), Chapter 4 (Article no. 31,32,33 and 35) and Chapter 7 (Article no. 43)
- 2) General Topology by S.Willard, Addison – Wesley Publishing Company (1970)
- 3) Introduction to Topology & Modern Analysis, G.F.Simons, Tata Mcgraw Hill (2004)

M.Sc. SEMESTER 2

Sub. Code: CMT-2004

Core Sub. 4: Methods in Partial Differential Equations

Unit 1

Surfaces and Curves in three dimensions, Simultaneous differential equations of the first order and the first degree in three variables, Methods of solutions of $dx/P + dy/Q + dz/R$, Orthogonal trajectories of a system of

curves on a surface. Pfaffian Differential forms and equations, Solution of Pfaffian differential equations in three variables, and Miscellaneous problems.

Unit 2

Partial differential equations, Origins of First-order partial differential equations, Linear equations of the first order, Integral Surfaces passing through a given curve, Surfaces orthogonal to a given system of surfaces.

Unit 3

Non-linear partial differential equations of the first order, Charpit's method, Special types of first order equations, Solutions satisfying the given conditions, Jacobi's method, and Miscellaneous problems.

Unit 4

The origin of second order equations, Linear partial differential equations with constant coefficients, and Equations with variable coefficients.

This course is covered by the relevant portions from the book 'Elements of Partial Differential Equations' by Ian Sneddon, McGraw-Hill Book Company.

Reference Books:-

1. Partial Differential Equations by F. John, Narosa Publishing Company, New Delhi, 1979.
2. Elementary Course in Partial Differential Equations by Amarnath, Narosa Publishing House, New Delhi, 1997.

M.Sc. SEMESTER 2

Sub. Code: **EMT-2001**

Elective Sub. 1: **Classical Mechanics -2**

Unit 1: The Rigid Body Equations of Motion

Angular momentum and kinetic energy of motion about a point, the inertia tensor and moment of inertia, the heavy symmetrical top with one point fixed.

Unit 2: Special Relativity in Classical Mechanics

The basic program of special relativity, The Lorentz transformation, Lorentz transformations in real four dimensional spaces, Further descriptions of the Lorentz transformation, Covariant four – dimensional formulations, The force and energy equations in relativistic mechanics.

Unit 3: Hamilton's equation of Motion

Derivation of Hamilton's equation of motion, Routh's procedure, derivation of Hamilton's equation from Hamilton's Principle, principle of least action, problem related to above topics.

Unit 4: Canonical transformations and Generating functions

Poisson's brackets and their properties, Hamilton-Jacobi theory, problem related to above topics.

The course is covered by the above topics from the book:

1. **Classical Mechanics** by H. Goldstein, 2nd Edition, Narosa Publishing House
2. **Classical Mechnaics** by C. R. Mondal, Prentice Hall of India Pvt. Ltd.